

# RiaSoR



RELIABILITY IN A SEA OF RISK

## Welcome to Day 1

*Developing an understanding of the VMEA framework*

# RiaSoR



RELIABILITY IN A SEA OF RISK

Elaine Buck  
Technical Manager  
EMEC

## **Day 1: 12:00-17:30**

*12:00 Lunch and registration*

13:00 Introduction/Background

13:30 VMEA framework

*15:00 Coffee break*

15:30 Exercises on VMEA: Paper clip fatigue

17:15 Wrap up

19:00 Dinner (optional)

## Day 2: 08:00-12:30

08:00 *Arrival*

08:30 Review of day 1

08:45 Case study: Moorings and foundations

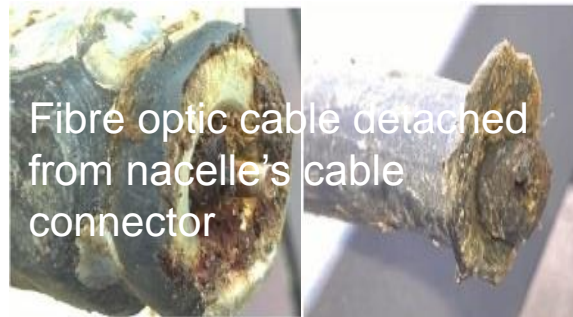
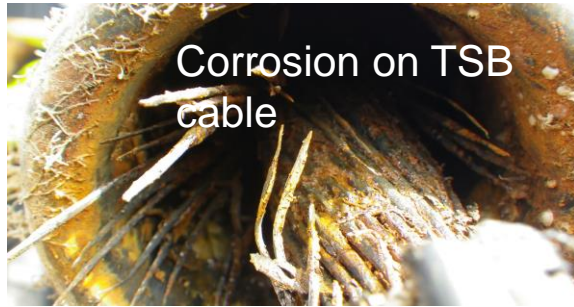
09:30 *Coffee break*

10:00 Case study: Structural component

11:00 Case study: Electrical component

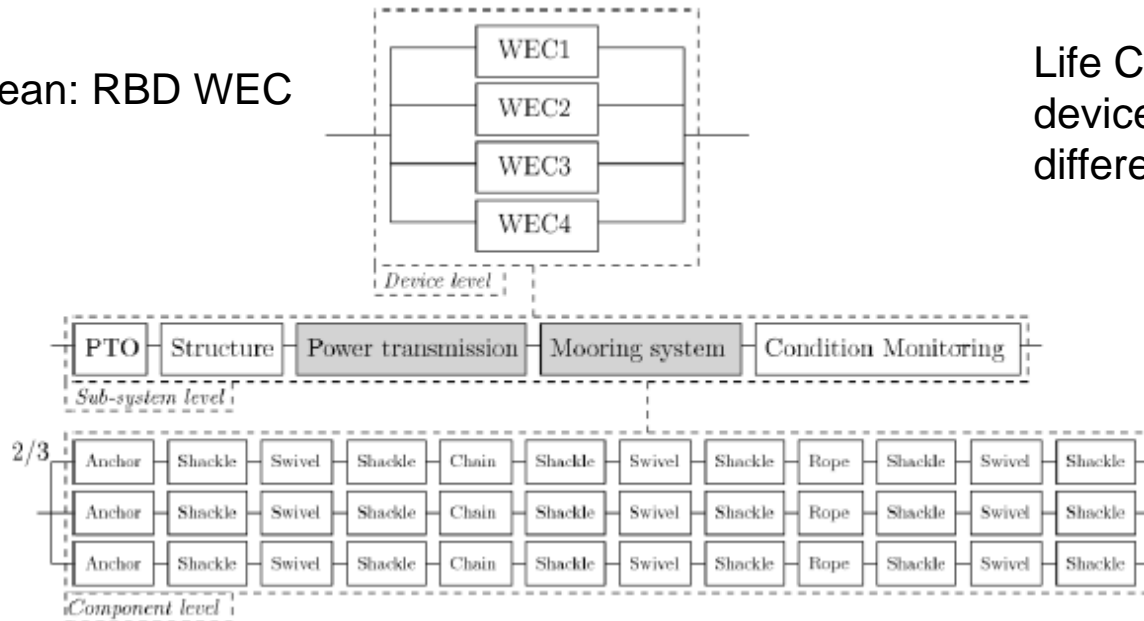
12:00 Summary of Key learning points

# Reliability Challenges



# Approaches/Tools

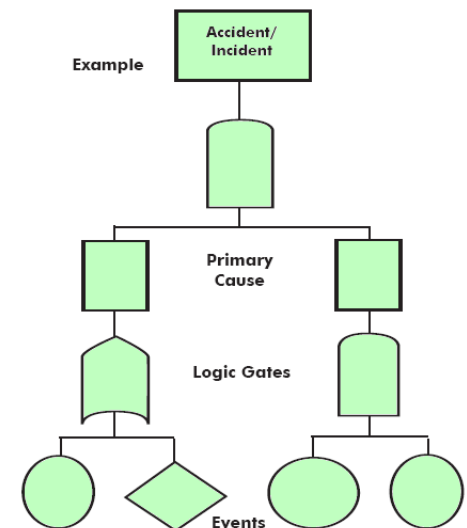
DTOcean: RBD WEC array



Life Cycle Cost (LCC) – best device options; comparison of different components

Fault Tree Analysis (FTA) – Failure analysis  
FMEA/FMECA – cause/effect

Availability Assessment – total availability of WEC/TEC system /time





Ocean ERANET funded (SE/SEA/InnovateUK)



1 year review of VMEA methodology, adaptation and application of VMEA for structural, moorings/foundations and electrical system subsystems.

Deliverables to industry:

1. Guideline
2. Educational / Instructional workshop and
3. Case studies on the above subsystem applications.

# RiaSoR

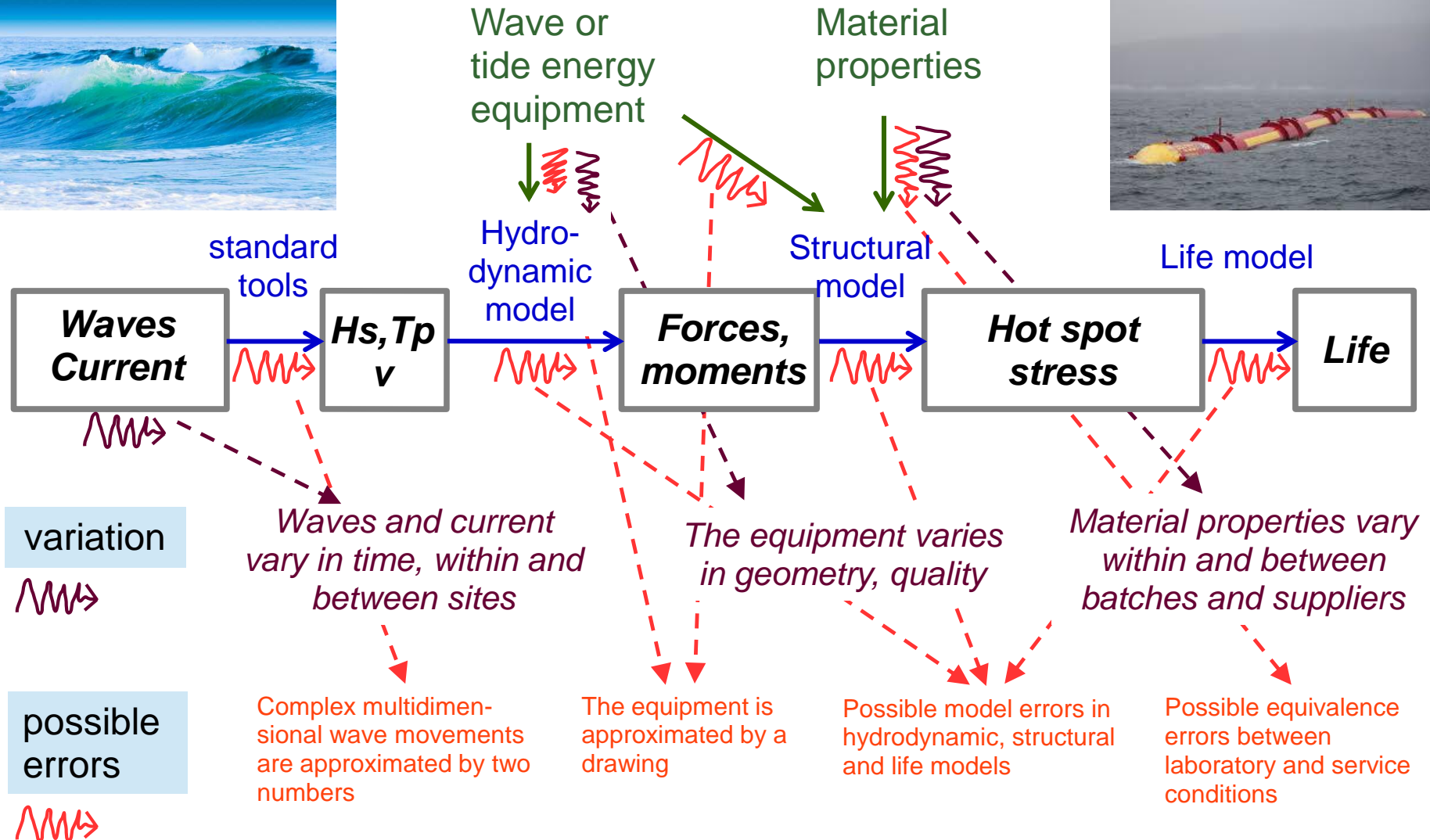


RELIABILITY IN A SEA OF RISK

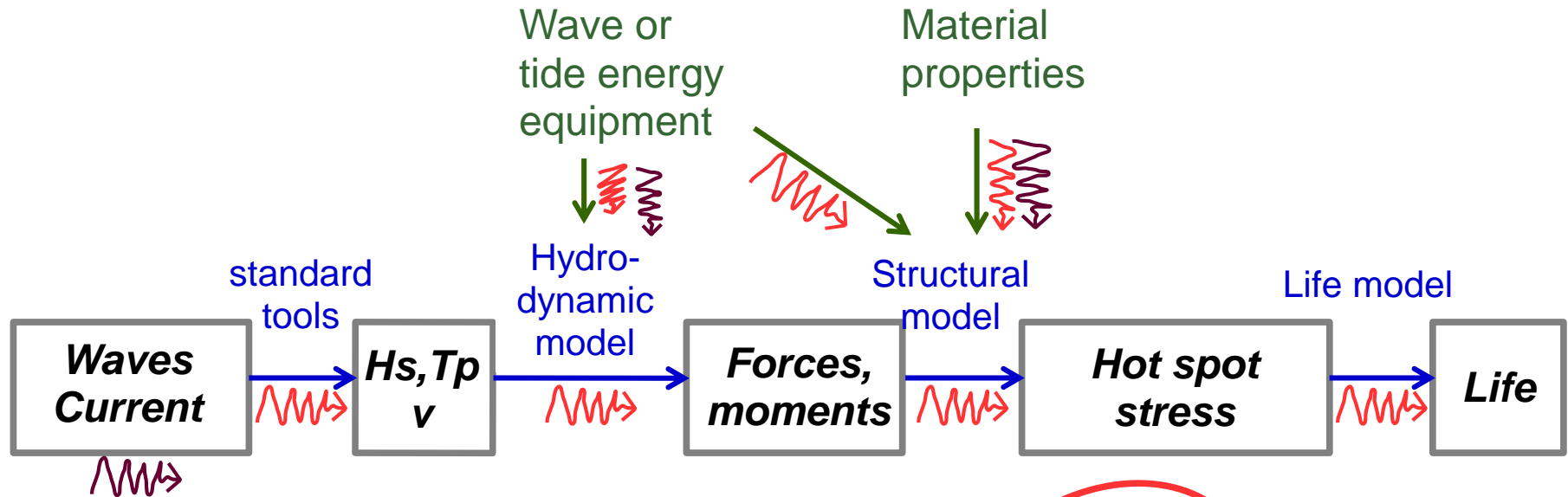
**Introduction to the VMEA concept**  
Thomas Svensson, PhD  
SP Technical Research Institute of Sweden



# Life assessment, overview

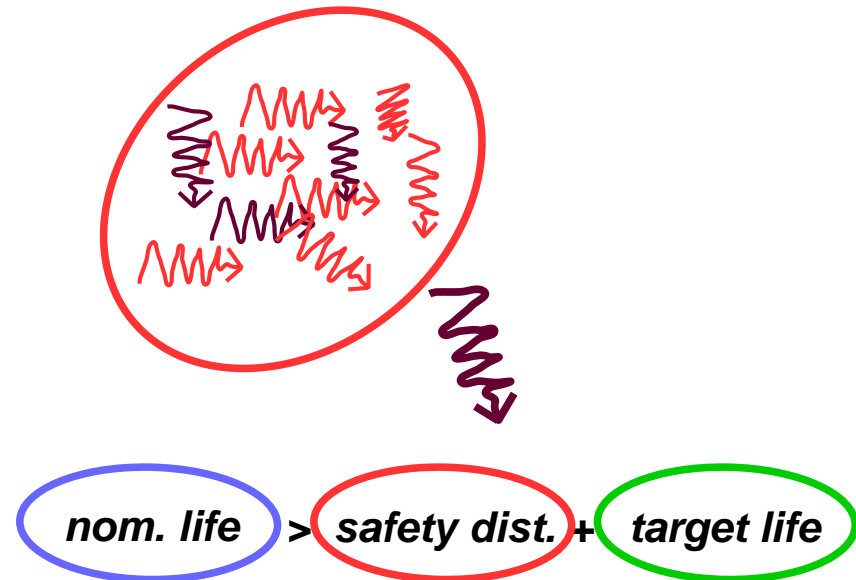


# VMEA uncertainty assessment

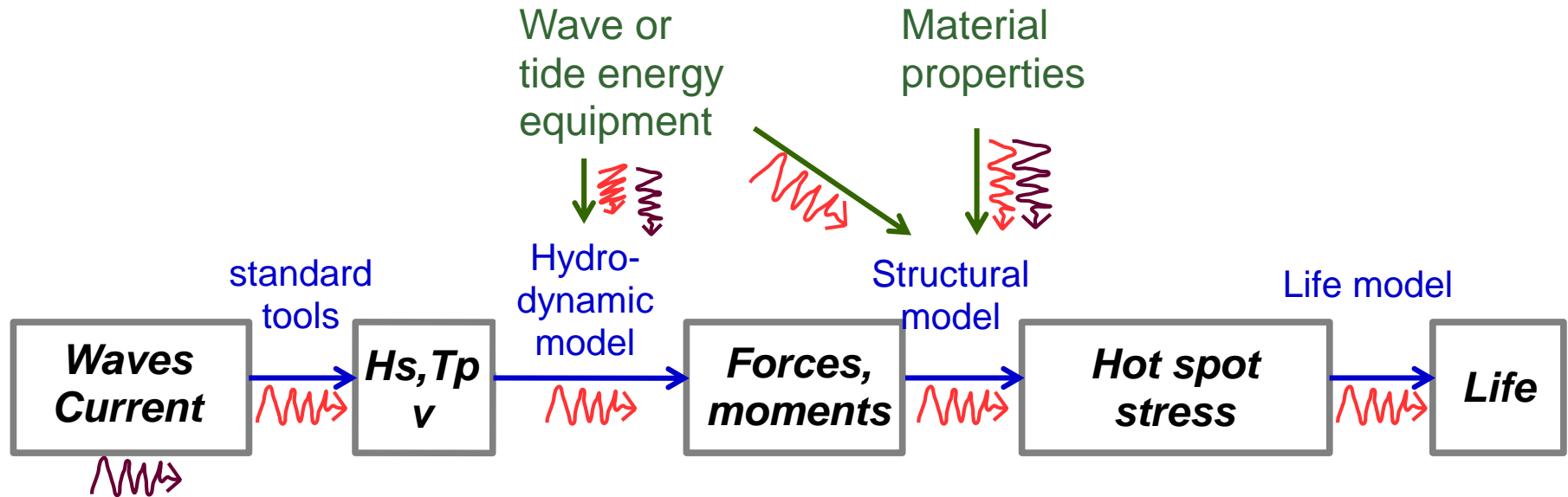


Both **possible errors** and **variation** must be taken into account when designing for life.

- The VMEA takes the **expected calculated life** as the starting point.
- The VMEA assigns a common **uncertainty metric** to each error and variation source.
- The VMEA then calculates an overall uncertainty for life which is used for the determination of a proper **safety factor**.



# VMEA uncertainty assessment



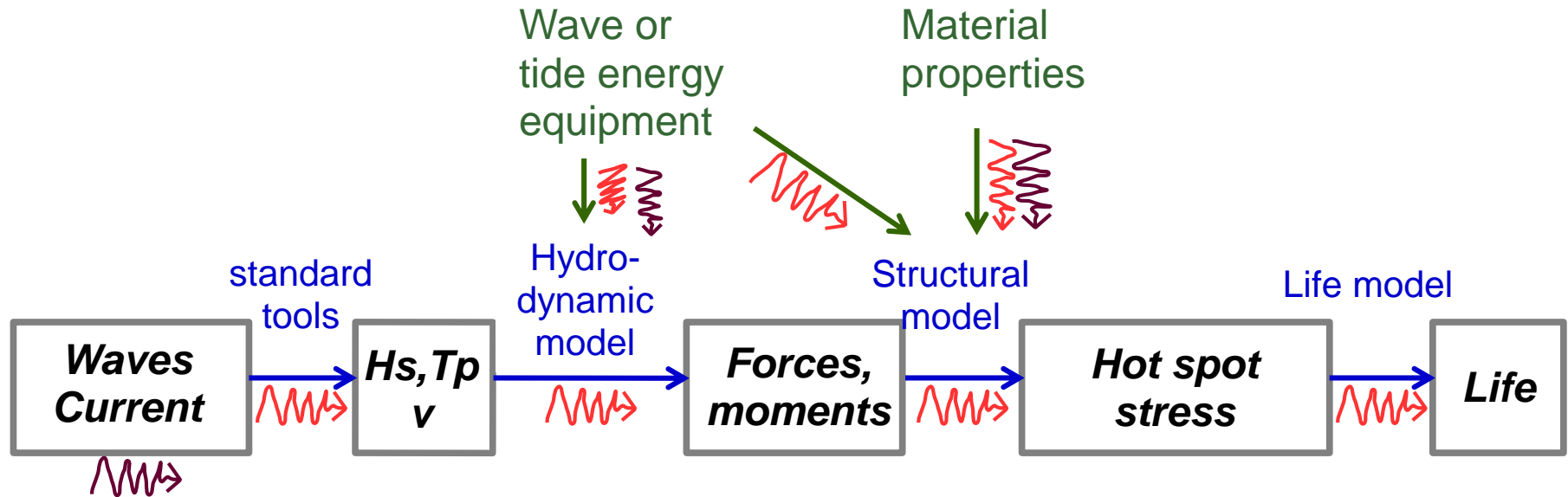
Common reliability approaches take height for uncertainties **in each step**:

- Variation is handled by using statistical safe quantiles or worst case scenarios.
- Model errors are handled by conservatism, choosing model variants that exaggerate severity and weakness.

This practice often results in oversized products since it is highly non-likely that the “worst case” occurs at each uncertain point.

This may be compensated by adjustments, but the methodology lacks control over the resulting reliability.

## The VMEA idea



The VMEA procedure is based on the assumption that all sources of variation and possible errors can be regarded as ***independent random variables***.

This means that the likelihood of a combination of “worst cases” can be controlled by statistical laws:

The overall uncertainty is calculated by adding the individual ***variance*** contributions:

***The uncertainty metrics are combined by their sum of squares***



# Beehive! Discuss...



What are the most important reliability issues in wave energy devices?

Examples of scatter sources?

Examples of possible error sources?

# RiaSoR



RELIABILITY IN A SEA OF RISK

## VMEA Methodology

Pär Johannesson, PhD

SP Technical Research Institute of Sweden

# VMEA (Variation Mode and Effect Analysis)

## Product Development

### Concept Phase

#### Basic VMEA

Only limited information is available

### Design Phase

#### Enhanced VMEA

More information is available

### Detailed Design Phase

#### Probabilistic VMEA

More detailed information about the structure and the sources of variation

Assign statistical variances to the different sources.

Evaluate the physical property, e.g. time to failure.

Example:

Evaluate the variation in life,  $N$ , of the most attractive design.

$$\ln(N) = f(T, P, \Delta, W) = f(x_1, x_2, x_3, x_4)$$

$$c_i = \frac{\partial_i f}{\partial x_i}, \quad \tau_i^2 = \text{Var}(x_i)$$

		Variation size $\tau_i$	Sensitivity $c_i$	Variation $c_i^2 \tau_i^2$
T	Temperature	0.28	1.1	0.09
P	Tension	0.22	3.8	0.70
$\Delta$	Tolerance	0.08	0.5	0.002
W	Wear	0.16	3.4	0.30
$\text{Var}(\ln(N)) = \sum c_i^2 \tau_i^2 = 1.09$				

Result:

Uncertainty in predicted life of the Belt.  
To improve the reliability, it would be most efficient to Improve the Tension properties.

## Outline

- VMEA in Product development
- Design Process for MECs
- Basic VMEA
  - Example: Mooring rope
- Probabilistic VMEA
  - Example: Mooring rope



## VMEA (Variation Mode and Effect Analysis) a Reliability Evaluation Method

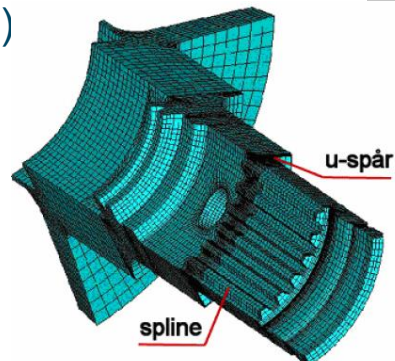
### Summary table of all uncertainties during the whole design process

- scatter of material properties
- statistical uncertainties
- geometry variation
- model uncertainties
- load uncertainties
- ...





### Which uncertainties dominates? (scatter or uncertainty?)

### How can uncertainties be decreased? (yielding best cost/profit)

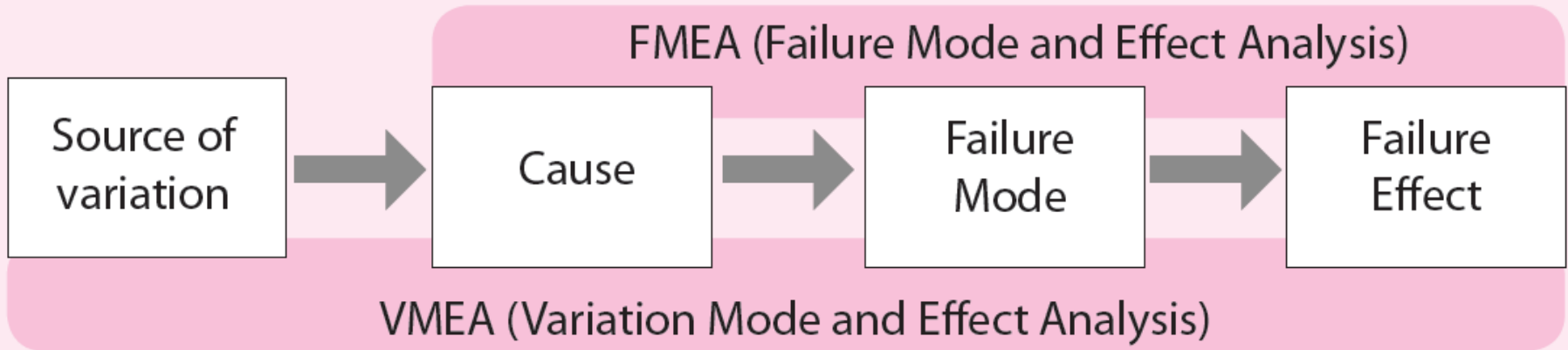
### Balanced complexity in models (don't overdo them)



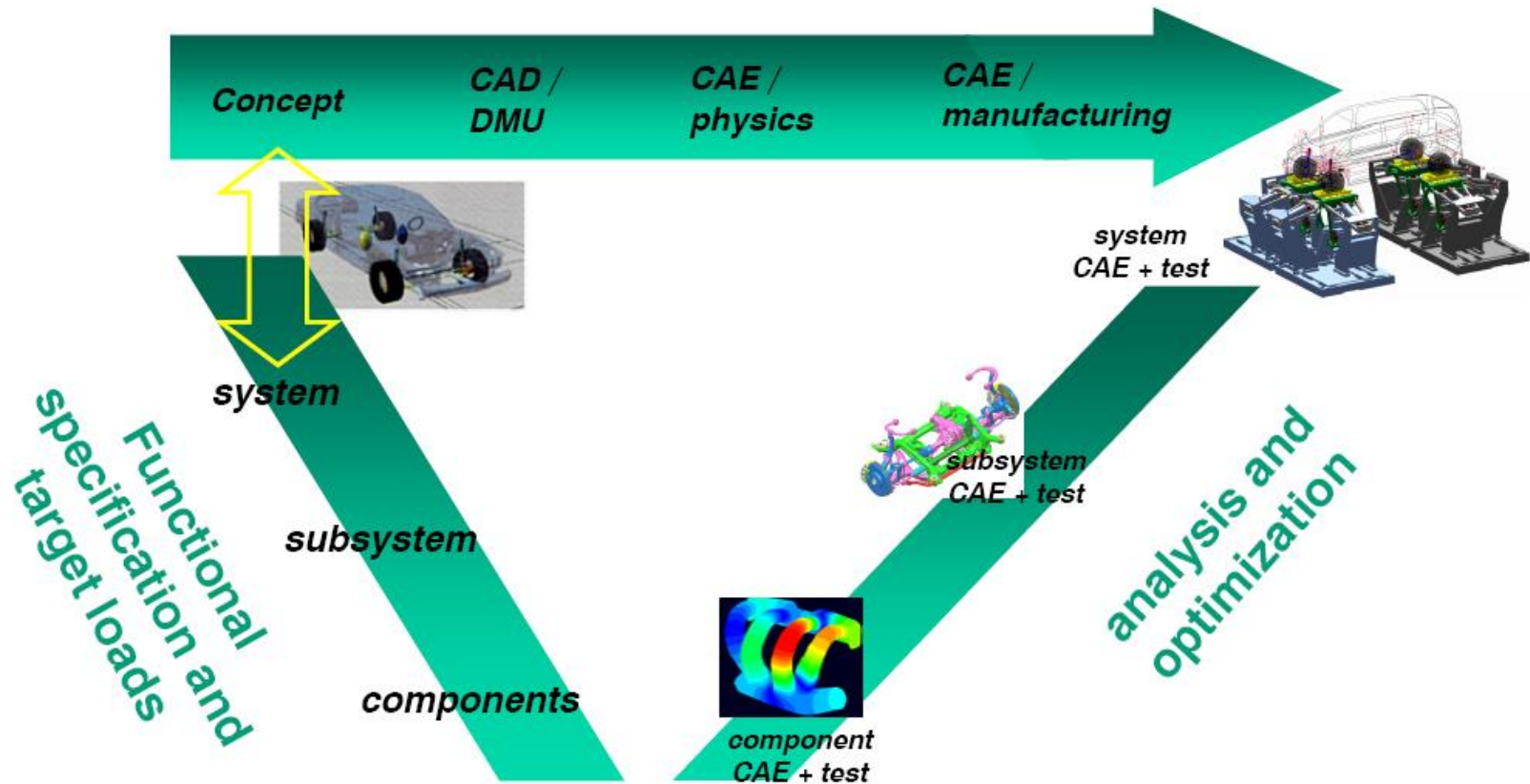
### Example: Volvo Aero, fatigue life evaluation

1. "First final design life predictions".			
Data and models	Influence on crack initiation life		
Type of scatter and uncertainty	scatter $\tau$	uncertainty $\delta$	total
Mtrl data (ln is normal-) distr.			<b>0.295</b>
-within 	0.291		
-between	0.050		
-statistical uncertainty Basq-Coff-Man		0.092	<b>0.092</b>
Geometry 			<b>0.400</b>
-tolerances	0.400		
Model uncertainty			<b>0.462</b>
-Basquin-Coffin-Manson-model		0.050	
-mean stress influence		0.075	
-multiaxiality, one-parameter model		0.183	
-stress analysis, plasticity 		0.049	
-stress analysis, model quality		0.096	
-sequence effects - linear damage		0.400	
-temperature effects		0	
-frequency influence		0	
Other uncertainties 			<b>0.234</b>
- Flight/service loads	-	0.234	
<b>Total</b>	<b>0.497</b>	<b>0.526</b>	<b>0.724</b>

## Unreliability is caused by Variation



- The FMEA method aims at finding all possible causes of failure.
- Studies have shown that most causes are triggered by unwanted variation.
- The VMEA method aims at finding all sources of variation that can trigger a failure mode.



# Design process for MECs

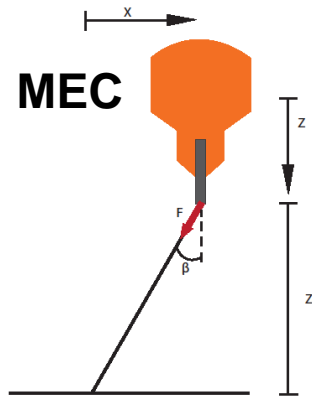
## Input: Sea loads

- Histogram of sea states,  $(H_s, T_p)$ .
- E.g. JONSWAP model for each sea state.



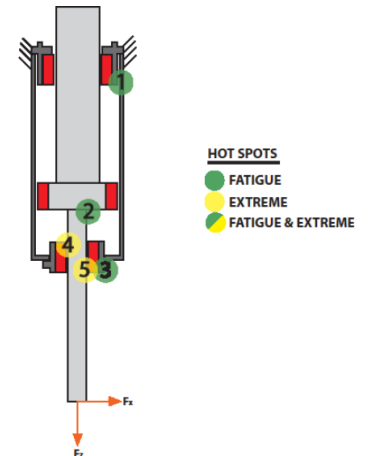
## Model: Sea loads to forces

- Model for simulating motion of the buoy and forces.



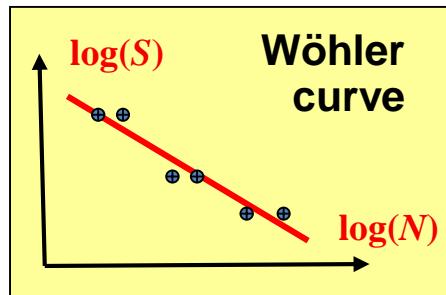
## Model: Forces to stress

- FEM
- Critical hotspots



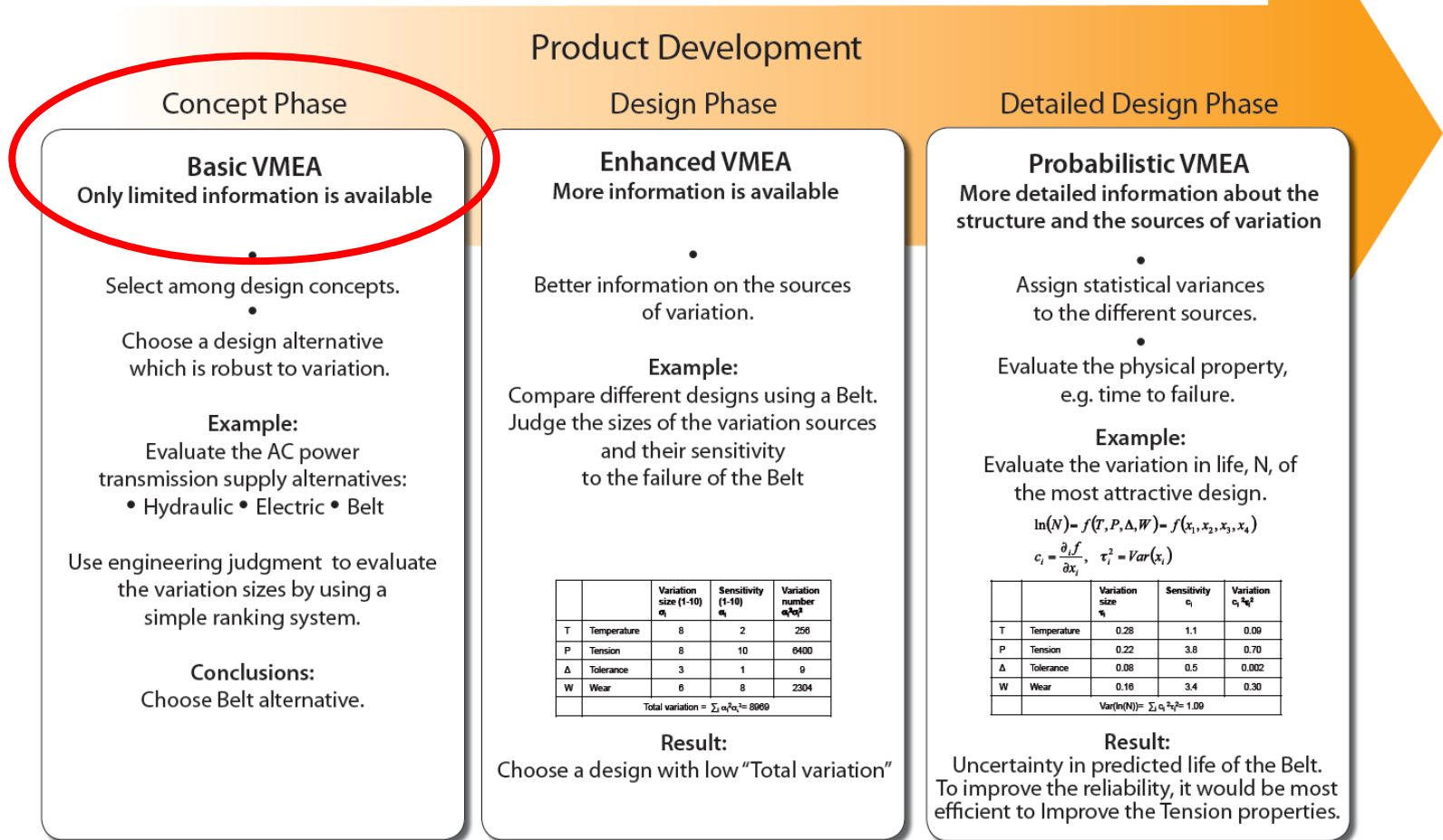
## Model: Fatigue life

- Wöhler curve
- Damage accumulation



# Basic VMEA

## VMEA (Variation Mode and Effect Analysis)



## 1. Target Function Definition

For example, the life of a component, the maximum stress or the largest defect.

## 2. Uncertainty Sources Identification

Identify all sources of uncertainty (scatter, statistical and model uncertainties).

## 3. Sensitivity Assessment

Evaluate the sensitivity coefficients of the sources of uncertainty.

## 4. Uncertainty Size Assessment

Quantify the size of the different sources of uncertainty.

## 5. Total Uncertainty Calculation

Combine the contributions from all uncertainty sources.

## 6. Reliability and Robustness Evaluation

Find the dominating uncertainties or derive safety factors.

## 7. Improvement Actions

Identify uncertainty sources that are candidates for improvement actions.



## 1. Target Function Definition

Define the target function, i.e. the property to be studied, which can be the life of a component, the maximum stress or the largest defect.



Waves4Power: <http://www.waves4power.com/>

### What do we want to study?

- Durability of a system/component  
=> Life requirement
- Survivability of a system/component  
=> Maximum stress



## 2. Uncertainty Sources Identification

Identify all sources of uncertainty that can have an impact on the target function.

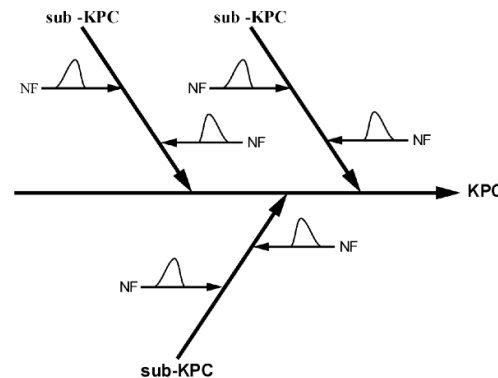
Different views and competences, cross-functional team of experts

### Some helpful tools:

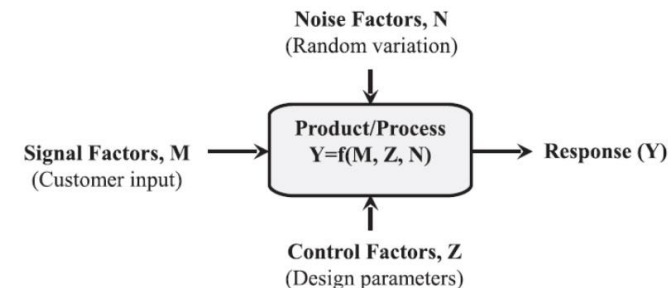
#### FMECA

POTENTIAL FAILURE MODE AND EFFECTS ANALYSIS										
Front Door L.H.										
FMEA Type					Process Responsibility		Body Engineering			
Item	1.1.1 - Front Door L.H.				Model Year(s)/Vehicle(s)		20XX/Lion 4dr/Wagon			
					Key Date		3/10/2015			
Core Team					A. Tate Body Engr, J. Smith - OC, R. James - Production, J. Jones - Maintenance					
Name / Function	Potential Failure Mode	Potential Effect(s) of Failure	SEV	Classification	Potential Cause(s) of Failure	OCC	Current Process Controls (Prevention)	Current Process Controls (Detection)	DET	BPN
Requirements										
1.1.1 - Front Door L.H.										
Op. 70 Manual application of wax inside door / cover inner door, lower surfaces with wax to specification thickness.	Insufficient wax coverage over specified surface	Allows integrity breach of inner door panel. Corroded interior lower door panels. Deteriorated life of door leading to: - Unsatisfactory appearance due to rust through paint over time - Impaired function of interior door hardware	7		Manually inserted spray head not inserted far enough	8		Visual check each hour - 1/shift for film thickness (depth meter) and coverage.	5	280
					Spray head clogged- Viscosity too high- Temperature too low- Pressure too low.	5	Test spray pattern at start-up and after idle periods, and preventive maintenance program to clean heads.	Visual check each hour - 1/shift for film thickness (depth meter) and coverage.	5	175
					Spray head deformed due to impact	2	Preventive maintenance program to maintain heads.	Visual check each hour - 1/shift for film thickness (depth meter) and coverage.	5	70

#### Fishbone diagram



#### P-diagram



# Identification of uncertainties

## Five categories of evil ...

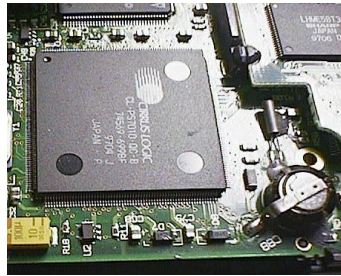
**Wearout** refers to deterioration of products due to ageing



**External environmental conditions** the products are exposed to



**Internal environmental conditions** the products are exposed to



**Customer "behaviour"** the products are exposed to



**Manufacturing imperfections** the products are exposed to



... in Automotive Industry ...

...and we **CANNOT** eliminate these factors!

# Beehive! Discuss...



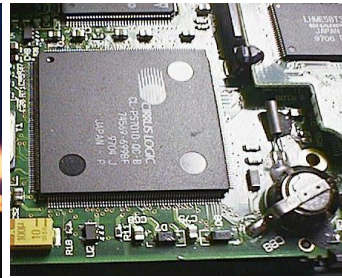
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Are these five categories relevant for Marine Energy Converters?



If so, what uncertainties can the categories represent?

Any examples?

## Five categories of evil ... for MECs

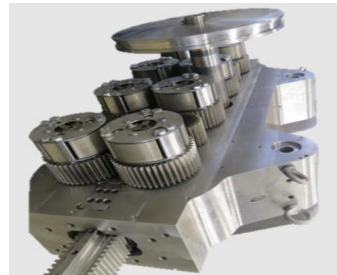
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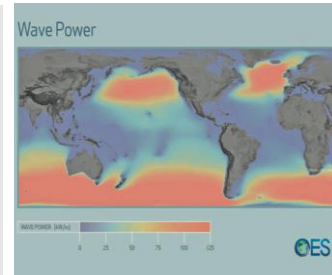
**External environmental conditions** the products are exposed to



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**Customer "behaviour"** the products are exposed to



**Manufacturing imperfections** the products are exposed to



# Basic VMEA

## Example: Mooring rope

### 1. Target Function Definition

The **target function** is the **life of the mooring rope**.

### 2. Uncertainty Sources Identification

The following uncertainties were identified:

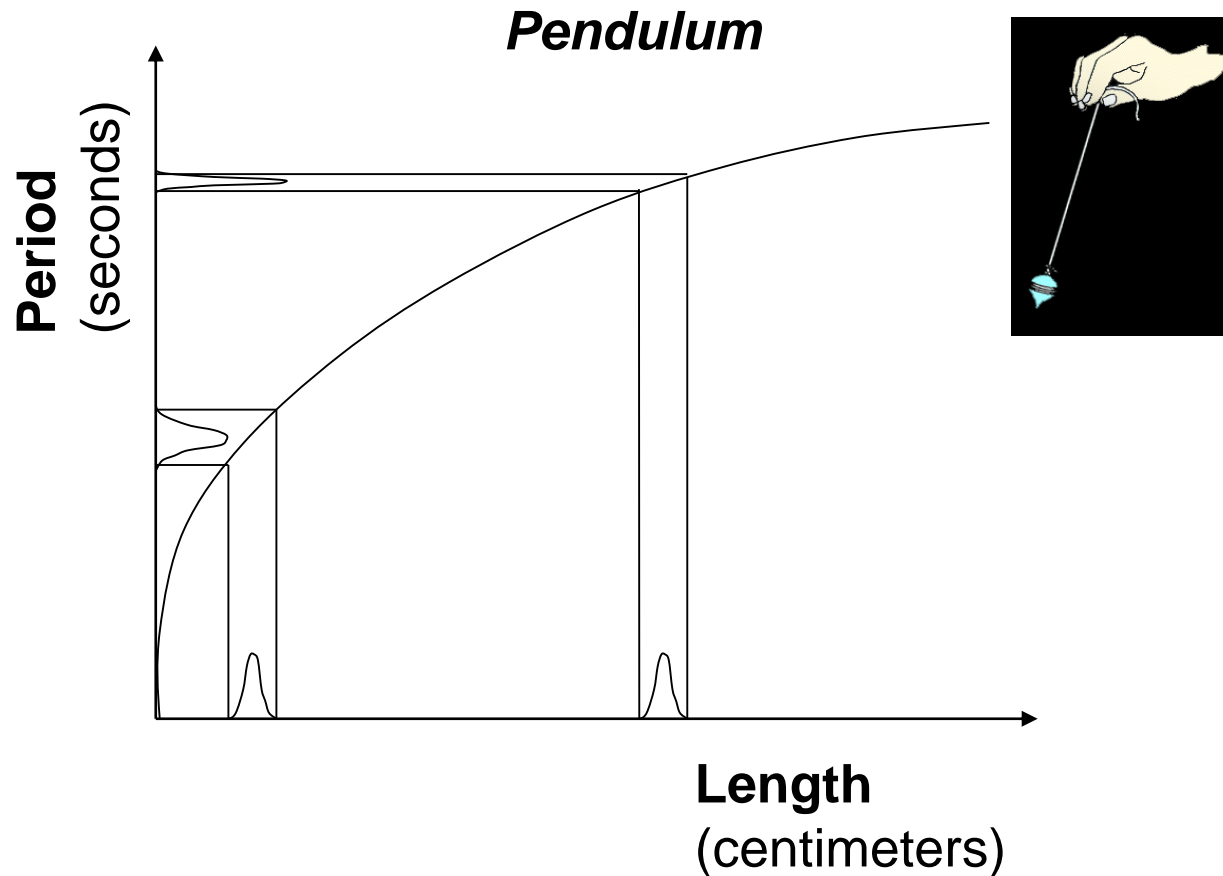
- Load variation
- Uncertainty in load assessment
- Scatter in fatigue life
- Uncertainty in the fatigue model
- Uncertainty due to influence of environment
- Geometry variations



**CorPower:**

[www.corpowerocean.com](http://www.corpowerocean.com)

## *Variation transmission – amplification and reduction*





# Basic VMEA

## Example: Mooring rope

### 3. Sensitivity Assessment.

Evaluate the sensitivity coefficients on a scale 1-10.

### 4. Uncertainty Size Assessment

Quantify the size of uncertainty on a scale 1-10.

Evaluate two alternatives: Steel wire & Polyester rope

Basic VMEA: Steel wire

Input		
Uncertainty sources	Sensitivity (1-10)	Uncertainty (1-10)
- Load variation	5	4
- Uncertainty in load assessment	5	6
- Scatter in fatigue life	5	5
- Uncertainty in the fatigue model	5	4
- Uncertainty due to environment	5	4
- Geometry variations	6	2
<b>Total uncertainty</b>		

Basic VMEA: Polyester rope

Input		
Uncertainty sources	Sensitivity (1-10)	Uncertainty (1-10)
- Load variation	5	4
- Uncertainty in load assessment	5	6
- Scatter in fatigue life	5	7
- Uncertainty in the fatigue model	5	8
- Uncertainty due to environment	5	3
- Geometry variations	6	3
<b>Total uncertainty</b>		



### 5. Total Uncertainty Calculation

Calculate the total resulting uncertainty in the output of the target function by combining the contributions from all uncertainty sources according to their sensitivities and sizes.

#### Basic VMEA: Steel wire

Input			Result		
Uncertainty sources	Sensitivity (1-10)	Uncertainty (1-10)	uncertainty	Variation contribution	
			$\tau_i = c_i \cdot \sigma_i$	VRPN	Portion
- Load variation	5	4	20	400	14%
- Uncertainty in load assessment	5	6	30	900	31%
- Scatter in fatigue life	5	5	25	625	22%
- Uncertainty in the fatigue model	5	4	20	400	14%
- Uncertainty due to environment	5	4	20	400	14%
- Geometry variations	6	2	12	144	5%
<b>Total uncertainty</b>			<b>54</b>	<b>2869</b>	<b>100%</b>

### VRPN = “Variation Risk Priority Number”

Total *VRPN* is calculated as the Sum of Squares (SS).

$$VRPN = \tau^2 = \tau_1^2 + \tau_2^2 + \tau_3^2 + \dots$$

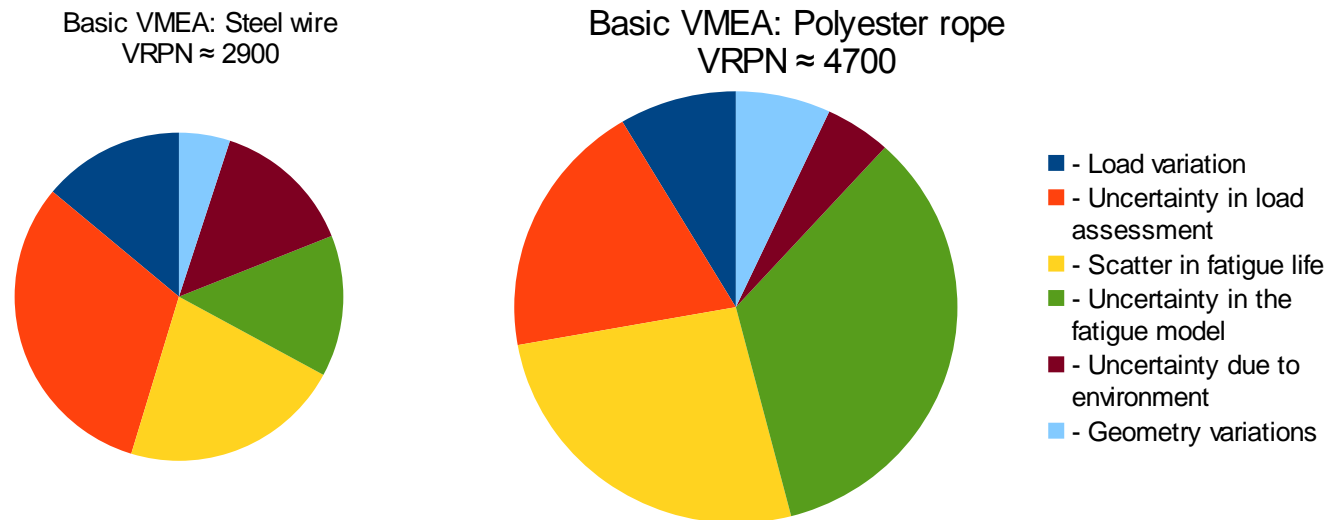
Total uncertainty  $\tau$  is calculated as the Root Sum of Squares (RSS).

### 6. Robustness Evaluation

Compare the two design concepts: Steel wire & Polyester rope.  
Polyester rope has larger uncertainties Steel wire concept due to large fatigue scatter and model uncertainty.

### 7. Improvement Actions

The steel wire is quite well understood; the main candidate for design.  
The polyester rope needs further investigations concerning fatigue.



# Probabilistic VMEA

## VMEA (Variation Mode and Effect Analysis)

### Concept Phase

#### Basic VMEA

Only limited information is available

- Select among design concepts.

- Choose a design alternative which is robust to variation.

#### Example:

Evaluate the AC power transmission supply alternatives:

- Hydraulic • Electric • Belt

Use engineering judgment to evaluate the variation sizes by using a simple ranking system.

#### Conclusions:

Choose Belt alternative.

### Product Development

### Design Phase

#### Enhanced VMEA

More information is available

- Better information on the sources of variation.

#### Example:

Compare different designs using a Belt. Judge the sizes of the variation sources and their sensitivity to the failure of the Belt

		Variation size (1-10) $\alpha_i$	Sensitivity (1-10) $\alpha_i$	Variation number $\alpha_i^2 \alpha_i^2$
T	Temperature	8	2	256
P	Tension	8	10	6400
A	Tolerance	3	1	9
W	Wear	6	8	2304
Total variation = $\sum \alpha_i^2 \alpha_i^2 = 8069$				

#### Result:

Choose a design with low "Total variation"

### Detailed Design Phase

#### Probabilistic VMEA

More detailed information about the structure and the sources of variation

- Assign statistical variances to the different sources.

- Evaluate the physical property, e.g. time to failure.

#### Example:

Evaluate the variation in life, N, of the most attractive design.

$$\ln(N) = f(T, P, \Delta, W) = f(x_1, x_2, x_3, x_4)$$

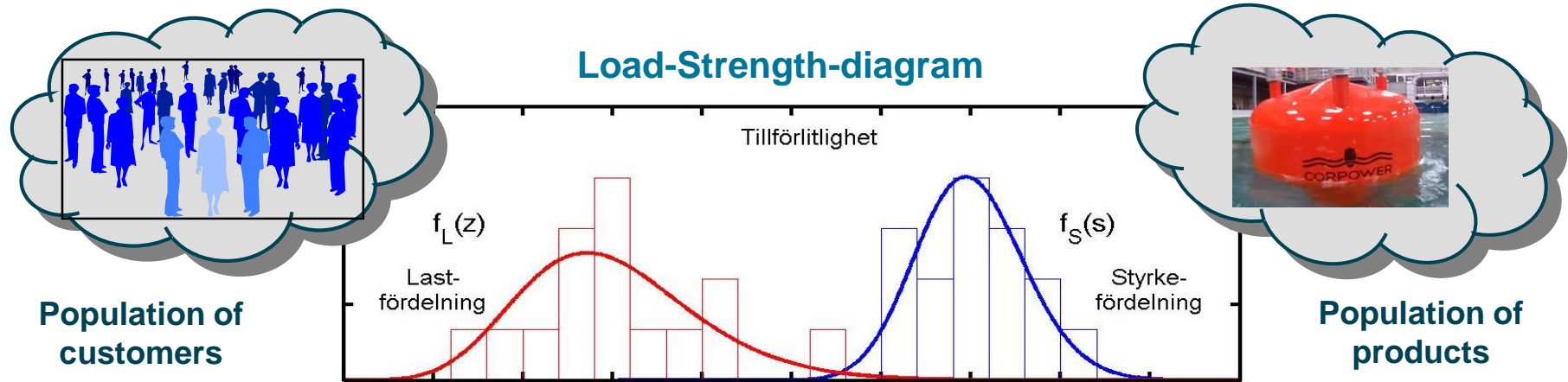
$$c_i = \frac{\partial f}{\partial x_i}, \quad \tau_i^2 = \text{Var}(x_i)$$

		Variation size $\alpha_i$	Sensitivity $\alpha_i$	Variation $\alpha_i^2 \alpha_i^2$
T	Temperature	0.28	1.1	0.09
P	Tension	0.22	3.8	0.70
A	Tolerance	0.08	0.5	0.002
W	Wear	0.16	3.4	0.30
Var(ln(N)) = $\sum \alpha_i^2 \alpha_i^2 = 1.09$				

#### Result:

Uncertainty in predicted life of the Belt. To improve the reliability, it would be most efficient to Improve the Tension properties.

# Reliability: Load-Strength Analysis



## Uncertainty in load

- Customer variation
- Usage and application area
- Environment (wave, wind, climate)
- Load estimation (ocean, test site)
- etc

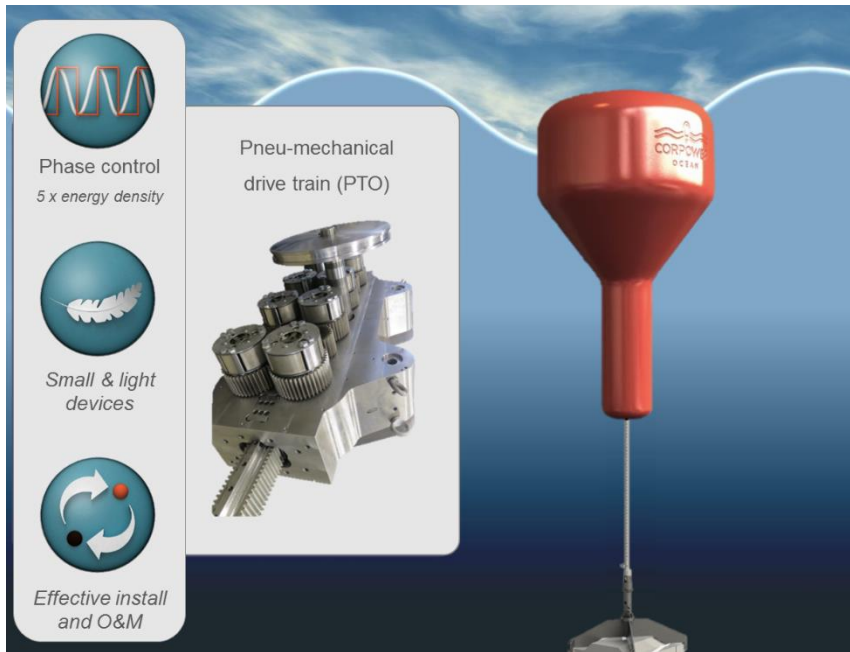
## Uncertainty in strength

- Material (type, surface, defects)
- Manufacturing
- Geometry (tolerances, surface roughness)
- Modelling (FEM, Wöhler, P-M, Neuber)
- etc

## P-VMEA: Mooring rope Target Function Definition

### 1. Target Function Definition

Define the target function, i.e. the property to be studied, which can be the life of a component, the maximum stress or the largest defect.



### What do we want to study?

- Durability of the mooring rope
- Life requirement, 20 years

CorPower: <http://www.corpowerocean.com>

## Design Process for MECs

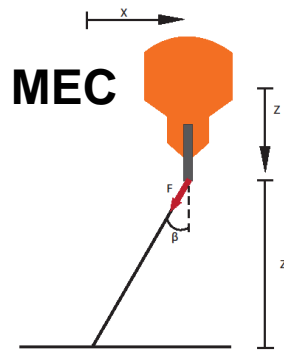
### Input: Sea loads

- Histogram of sea states,  $(H_s, T_p)$ .
- JONSWAP model for each sea state.



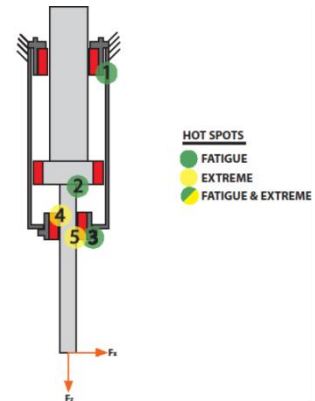
### Model: Sea loads to forces

- Model for simulating motion of the buoy and forces.



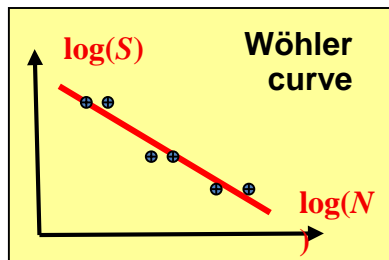
### Model: Forces to stress

- FEM
- Identify hotspots



### Model: Fatigue life

- Wöhler curve
- Damage accumulation



## Five categories of evil ...

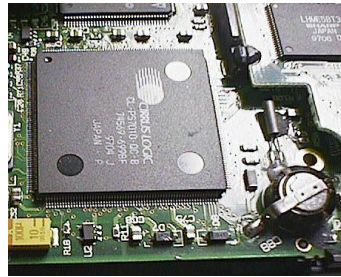
**Wearout** refers to deterioration of products due to ageing



**External environmental conditions** the products are exposed to



**Internal environmental conditions** the products are exposed to



**Customer "behaviour"** the products are exposed to



**Manufacturing imperfections** the products are exposed to



- Scatter
- Statistical uncertainty
- Model uncertainty



**CANNOT** be eliminated!

**CAN** be reduced or eliminated!

... by better knowledge or more data.



## Probabilistic VMEA

### Sensitivity & uncertainty size assessment

The **metrics** in the probabilistic VMEA are:

1. **Sensitivities** by means of mathematical **sensitivity coefficients**,
  2. **Uncertainty** by means of **statistical standard deviations**
- instead of 1-1- scales in the basic VMEA.

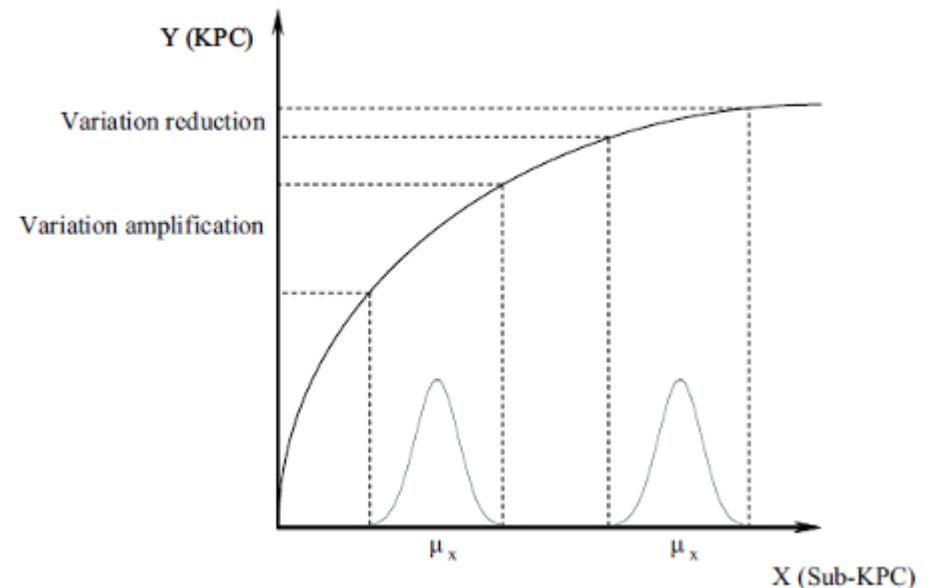
For a target function

$$Y = f(X_1, X_2, X_3, \dots)$$

1. the **sensitivity coefficients** is

$$c_i = \frac{\partial f}{\partial X_i}$$

2. the **uncertainty** is  
the **standard deviation**  
 $\tau_i = std(X_i)$



# P-VMEA: Mooring rope

## Total uncertainty calculation: VMEA Table

Input						Result		
Uncertainty components	Scatter	Uncert.	Sensitivity coefficient c	t-correction factor t	standard deviation s	Scatter	Uncertainty	Total
<b>Strength</b>								
Strength scatter	x		0,208	1,060	0,540	0,119		
Statistical uncert. strength		x	0,208	1,000	0,200		0,042	
Adjustment uncertainty CA/VA		x	0,208	1,000	0,100		0,021	
Reference data relevance		x	1,000	1,000	0,100		0,100	
Mean value influence		x	1,000	1,000	0,050		0,050	
Laboratory uncertainty		x	1,000	1,000	0,029		0,029	
<b>Total Strength uncertainty</b>						<b>0,119</b>	<b>0,125</b>	<b>0,172</b>
<b>Load</b>								
Pool measurements, scatter	x		1,000	1,300	0,040	0,052		
Scaling		x	1,000	1,000	0,012		0,012	
Distribution of Hf		x	1,000	1,000	0,014		0,014	
Model uncertainty		x	1,000	1,000	0,023		0,023	
Friction		x	1,000	1,000	0,029		0,029	
<b>Total Load uncertainty</b>						<b>0,052</b>	<b>0,041</b>	<b>0,066</b>
Wöhler Exponent		x	0,200	1,000	0,500		0,100	
<b>Total Exponent uncertainty</b>						<b>0,000</b>	<b>0,100</b>	<b>0,100</b>
<b>Total uncertainty</b>						<b>0,130</b>	<b>0,165</b>	<b>0,210</b>

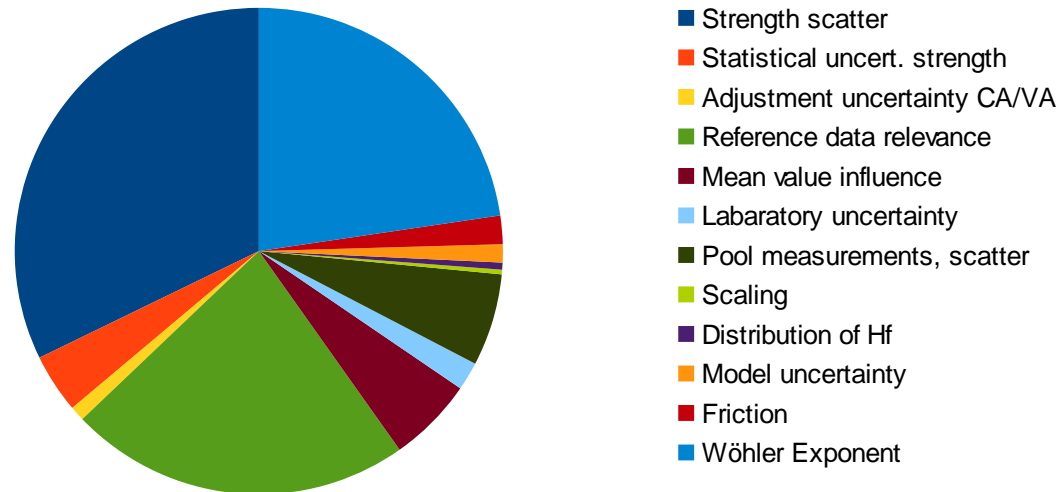
$$\text{Total uncertainty: } \tau = \sqrt{\tau_1^2 + \tau_2^2 + \tau_3^2 + \dots} = 0.210$$

# P-VMEA: Mooring rope

## Uncertainty contributions

### Probabilistic VMEA for steel wire

#### Pie chart of uncertainty contributions



The **three dominating sources** are:

1. Strength scatter
2. Reference data relevance (uncertainty)
3. Wöhler exponent (uncertainty)

# P-VMEA: Mooring rope Reliability Evaluation

Total uncertainty						0,130	0,165	0,210
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$$\text{Total uncertainty: } \tau = \sqrt{\tau_1^2 + \tau_2^2 + \tau_3^2 + \dots} = 0.210$$

## Reliability Evaluation

wire diameter (mm) 110

Input		Result	
Median strength [MN]	2,25	Safety factor	1,41
Median Load [MN]	1,60		

Result (log -s scale)	
Strength, mS	0,81
Load, mL	0,47
Distance	0,34

**Load-Strength, Nominal values:**  $\ln S_{nom} - \ln L_{nom} = 0.81 - 0.47 = 0.34$

Evaluation - Extra safely factor	Variation safety factor	1,41	Variation dist.	0,34
Required extra safety factor	1	1,00	Extra dist.	0,00

<b>95% prediction interval:</b>	<b>Safety margin</b> $1.64 \cdot \tau = 0.34$	<b>Safety factor</b> $\exp(1.64 \cdot \tau) = 1.41$
<b>Extra safety factor:</b>	$\delta_E = 0$	$\gamma_E = \exp(0) = 1$

<b>Load-Strength judgement:</b>	Nominal: $\ln S_{nom} - \ln L_{nom} = 0.81 - 0.47 = 0.34$
	Requirement: $1.64 \cdot \tau + \delta_E = 0.34$

### 7. Improvement Actions

Identify uncertainty sources that are candidates for improvement actions.

#### Improvement Actions:

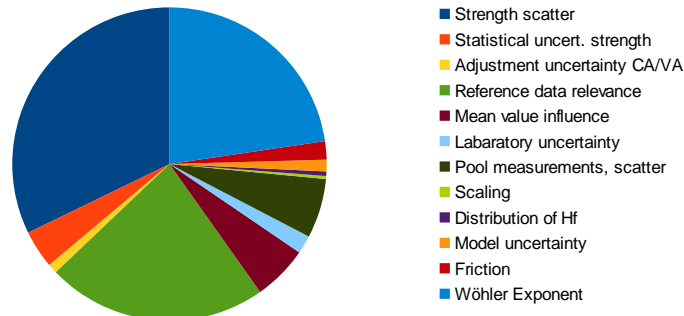
Design change:

Wave spring replaces latching mechanism

=> Reduce loads

The largest uncertainties are connected to the strength, possible improvements:

- specifying wire rope quality, and
- arrange laboratory wire tests.



**CorPower:**

[www.corpowerocean.com](http://www.corpowerocean.com)

## VMEA (Variation Mode and Effect Analysis)

### Product Development

#### Concept Phase

##### Basic VMEA

Only limited information is available

- Select among design concepts.

- Choose a design alternative which is robust to variation.

##### Example:

Evaluate the AC power transmission supply alternatives:

- Hydraulic • Electric • Belt

Use engineering judgment to evaluate the variation sizes by using a simple ranking system.

##### Conclusions:

Choose Belt alternative.

#### Design Phase

##### Enhanced VMEA

More information is available

- Better information on the sources of variation.

##### Example:

Compare different designs using a Belt. Judge the sizes of the variation sources and their sensitivity to the failure of the Belt

		Variation size (1-10) $\alpha_i$	Sensitivity (1-10) $\alpha_i$	Variation number $\alpha_i^2 \alpha_i^2$
T	Temperature	8	2	256
P	Tension	8	10	6400
A	Tolerance	3	1	9
W	Wear	6	8	2304
Total variation = $\sum \alpha_i^2 \alpha_i^2 = 8069$				

##### Result:

Choose a design with low "Total variation"

#### Detailed Design Phase

##### Probabilistic VMEA

More detailed information about the structure and the sources of variation

- Assign statistical variances to the different sources.

- Evaluate the physical property, e.g. time to failure.

##### Example:

Evaluate the variation in life, N, of the most attractive design.

$$\ln(N) = f(T, P, \Delta, W) = f(x_1, x_2, x_3, x_4)$$

$$c_i = \frac{\partial f}{\partial x_i}, \quad \tau_i^2 = \text{Var}(x_i)$$

		Variation size $\alpha_i$	Sensitivity $\alpha_i$	Variation $\alpha_i^2 \alpha_i^2$
T	Temperature	0.28	1.1	0.09
P	Tension	0.22	3.8	0.70
A	Tolerance	0.08	0.5	0.002
W	Wear	0.16	3.4	0.30
Var(ln(N)) = $\sum \alpha_i^2 \alpha_i^2 = 1.09$				

##### Result:

Uncertainty in predicted life of the Belt. To improve the reliability, it would be most efficient to Improve the Tension properties.



# Thanks for your attention!



## **RISE – Research Institutes of Sweden**

SP, Swedish ICT, and Innventia have merged, with the aim of together creating a more united institute sector and becoming a stronger innovation partner for both the Swedish business community and broader society. In the new year we will officially change our name to RISE. Pia Sandvik is the MD of the new macro-institute.

# RiaSoR



RELIABILITY IN A SEA OF RISK

## Coffee Break

15:00 – 15:30

# Exercise: Paper clip fatigue

## Objective:

Study the reliability of paperclips with regard to their bending strength.

## Task:

- Each participant bends a paperclip 30 degrees back and forth until it fails. Count the number of half bending reversals.
- Do the same test on a new paperclip, now by bending 45 degrees back and forth.

39			
A	B	C	
		Target life	
		Max variation in usage: +/-	
<b>Number of half reversals to failure</b>			<b>Logs</b>
<b>30 degrees</b>	<b>45 degrees</b>		<b>30 deg</b>
140	47		
49	45		
44	6		
72	13		
54	8		
17	26		

- As a group, record the results on the prepared spreadsheet.

The spreadsheet will calculate the:

- Log lives,
- Mean values and
- Standard deviation.

- As a group, conduct a VMEA analysis by inputting the results into the VMEA sheet.

# Exercise: Paper clip fatigue

	<b>30 degrees</b>	<b>45 degrees</b>	
<i>mean</i>	4.0	2.9	
<i>standard deviation</i>	0.69	0.88	
<i>number of obs.</i>	6	6	
Fatigue strength at 30 degrees	<b>4.0</b>		
Log life scatter	<b>0.69</b>		
t-correction	<b>1.3</b>		
Log life scatter pooled	0.79		
t-correction pooled	1.1		
Fatigue strength at 45 degrees	2.9		
Sensitivity coefficient	<b>0.071</b>		
Load variation (sd)	<b>5.77</b>		
Target log life	<b>1.61</b>		

$$= \text{tinv}(0.05,5)/1.96$$

$$= (4.0-2.9)/15$$

$$= 10/\text{sqrt}(3)$$

# Exercise: Paper clip fatigue

	<b>30 degrees</b>	<b>45 degrees</b>
mean	4.0	2.9
standard deviation	0.69	0.88
number of obs.	6	6
Fatigue strength at 30 degrees	<b>4.0</b>	
Log life scatter	<b>0.69</b>	
t-correction	<b>1.3</b>	
Log life scatter pooled	0.79	
t-correction pooled	1.1	
Fatigue strength at 45 degrees	2.9	
Sensitivity coefficient	<b>0.071</b>	
Load variation (sd)	<b>5.77</b>	
Target log life	<b>1.61</b>	

The first row in the VMEA sheet represents uncertainty due to scatter.

1. The calculated standard deviation “Log life scatter” is placed in the s-cell.
2. The t-correction number is put in the t-cell.
3. The sensitivity coefficient is put to unity.
4. The type of uncertainty is marked as a cross in the correct cell.

Input						Result		
	scatter	uncert.	Sensitivity coefficient c	correction factor t	standard deviation s	Scatter	Uncertainty	Total
Uncertainty components								
Strength								
Scatter								
Nominal fatigue strength								
Total Strength uncertainty						0.000	0.000	0.000
Load								
Variation in usage								
Total Load uncertainty						0.000	0.000	0.000
Total uncertainty						0.000	0.000	0.000

# Exercise: Paper clip fatigue

	30 degrees	45 degrees
mean	4.0	2.9
standard deviation	0.69	0.88
number of obs.	6	6
Fatigue strength at 30 degrees	4.0	
Log life scatter	0.69	
t-correction	1.3	
Log life scatter pooled	0.79	
t-correction pooled	1.1	
Fatigue strength at 45 degrees	2.9	
Sensitivity coefficient	0.071	
Load variation (sd)	5.77	
Target log life	1.61	

The second row in the VMEA sheet represents uncertainty in the estimated life.

1. The standard deviation is divided by the square root of the number of tests and put in the s column.
2. The t-correction number is the same as for the scatter
3. The sensitivity coefficient is put to unity.
4. The type of uncertainty is marked as a cross in the correct cell.

Input						Result		
	scatter	uncert.	Sensitivity coefficient c	correction factor t	standard deviation s	Scatter	Uncertainty	Total
Uncertainty components								
Strength								
Scatter								
Nominal fatigue strength								
Total Strength uncertainty						0.000	0.000	0.000
Load								
Variation in usage								
Total Load uncertainty						0.000	0.000	0.000
Total uncertainty						0.000	0.000	0.000



# Exercise: Paper clip fatigue

	<b>30 degrees</b>	<b>45 degrees</b>
mean	4.0	2.9
standard deviation	0.69	0.88
number of obs.	6	6
Fatigue strength at 30 degrees	<b>4.0</b>	
Log life scatter	<b>0.69</b>	
t-correction	<b>1.3</b>	
Log life scatter pooled	0.79	
t-correction pooled	1.1	
Fatigue strength at 45 degrees	2.9	
Sensitivity coefficient	<b>0.071</b>	
Load variation (sd)	<b>5.77</b>	
Target log life	<b>1.61</b>	

The first row under the Load heading represents the variation in usage

1. The Load variation number is put in the s-cell.
2. The t-correction number is unity
3. The Sensitivity coefficient is put in the c column.
4. The type of uncertainty is marked as a cross in the correct cell.

Input						Result		
	scatter	uncert.	Sensitivity coefficient c	correction factor t	standard deviation s	Scatter	Uncertainty	Total
<b>Uncertainty components</b>								
<b>Strength</b>								
Scatter								
Nominal fatigue strength								
<b>Total Strength uncertainty</b>						0.000	0.000	0.000
<b>Load</b>								
Variation in usage								
<b>Total Load uncertainty</b>						0.000	0.000	0.000
<b>Total uncertainty</b>						0.000	0.000	0.000

# Exercise: Paper clip fatigue

Reliability Evaluation						
Input			Result		Result (log-scale)	
Median life (reversals)		1	Safety factor	1,00	Life	0,00
Target life (reversals)		1			Target life	0,00
					Distance	0,00
Evaluation - Extra safety factor			Variation safety factor	1,00	Variation dis	0,00
Required extra safety factor		2	Extra safety factor	1,00	Extra dist.	0,00

- The fatigue strength at 30 degrees is put in the life cell (log scale).
- The target log life is put in the Target life cell.
- The spreadsheet then calculates the nominal safety factor and compares it with the calculated statistical safety factor and the demanded extra safety factor.

# RiaSoR



RELIABILITY IN A SEA OF RISK

## Day 1

Review and wrap up

# RiaSoR



RELIABILITY IN A SEA OF RISK

Please join us for tea at The Dhabba,  
44 Candleriggs, Merchant City, at 7pm.

**08:00 Arrival for Day 2**